

Number Problems

1. The sum of two numbers is 48. If the smaller number is subtracted from the larger, the difference is 12. Find the numbers.

The #'s are 30 + 18.

$$\begin{array}{rcl} x - \text{larger \#} & x + y = 48 & \frac{2x}{2} = \frac{60}{2} \\ y - \text{smaller \#} & + x - y = 12 & \frac{-30}{-30} \quad \frac{-30}{-30} \\ \hline & 2x = 60 & x = 30 \end{array}$$

$$\begin{array}{rcl} 30 + y = 48 & & \\ -30 & & -30 \\ \hline y = 18 & & \end{array}$$

2. One number is 4 more than half of another. The difference between the two numbers is 2. Find the numbers.

The #'s are 4 + 6.

$$\begin{array}{rcl} x - 1\text{st \#} & x = 4 + \frac{1}{2}y & 4 + \frac{1}{2}y - y = 2 \\ y - 2\text{nd \#} & x - y = 2 & -4 \quad -\frac{1}{2}y = -2 - 2 \\ & & -2 \quad (-\frac{1}{2})y = (-2) - 2 \\ & & y = 4 \end{array}$$

$$x = 4 + \frac{1}{2}(4) = 6$$

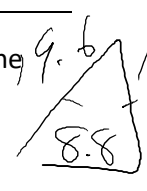
3. One positive number equals 3 times another number. The difference between the numbers is 1. Find the numbers.

The numbers are 1.5 and 0.5.

$$\begin{array}{rcl} x - 1\text{st \#} & x = 3y & x - y = 1 \\ y - 2\text{nd \#} & 3y - y = 1 & x = 3(\frac{1}{2}) \\ & 2y = 1 & x = 1.5 \\ & y = \frac{1}{2} & \end{array}$$

Perimeter Problems

4. The perimeter of an isosceles triangle is 48 in. The length of the base is 1 in less than half the length of one of the two equal sides. Find the lengths of the sides of the triangle.



$$\begin{array}{rcl} x - \text{equal side} & 2x + y = 48 & 2x + \frac{1}{2}x - 1 = 48 \\ y - \text{base} & y = \frac{1}{2}x - 1 & +1 \quad +1 \\ & y = \frac{1}{2}(19.6) - 1 & \frac{2.5x}{2.5} = \frac{49}{2.5} \\ & y = 8.8 & x = 19.6 \end{array}$$

5. The perimeter of a rectangle is 10 m. Twice the width is equal to one-half the length. Find the length and width.

$$\begin{array}{rcl} w - \text{width} & 2w + 2l = 10 & \frac{1}{2}l + 2l = 10 \\ l - \text{length} & 2w = \frac{1}{2}l & 2w = \frac{1}{2}(4) \\ & & \frac{2w}{2} = \frac{2}{2} \\ & & w = 1 \end{array}$$

The length is 4m and the width is 1m.

6. The perimeter of a triangular sign is 21 ft. If the lengths of two sides are equal and the third side is 3 ft longer than one of the equal sides, find the lengths of the three sides.

$$\begin{array}{rcl} x - \text{length of 2 sides} & 2x + y = 21 & 2x + x + 3 = 21 \\ y - \text{longer side} & y = x + 3 & -3 \quad -3 \\ & y = 6 + 3 & \frac{3x}{3} = \frac{18}{3} \\ & y = 9 & x = 6 \end{array}$$

The sides are 6ft, 6ft, + 9ft.

Money & Fund Raising Problems

7. Lorena has 26 coins in nickels and quarters, which are worth a total of \$3.10. How many of each coin does she have?

$$\begin{array}{l} n - \# \text{ of nickels} \\ q - \# \text{ of quarters} \end{array}$$

$$4(0.05n + 0.25q) = (3.10) \quad 4 \quad \begin{array}{r} 0.8n = 13.6 \\ \hline 0.8 \quad 0.8 \\ n = 17 \end{array}$$

$$\begin{array}{r} n + q = 26 \\ -(0.20n + q = 12.40) \\ \hline 0.8n = 13.6 \end{array}$$

9 quarters and 17 nickels.

8. To raise funds, the math club sells two kinds of raffle tickets, some for \$6, others for \$1.50. Sales for both amounted to \$822. If 371 tickets were sold, how many were \$1.50 tickets?

$$\begin{array}{l} x - \# \text{ of } \$6 \text{ tickets} \\ y - \# \text{ of } \$1.50 \text{ tickets} \end{array}$$

$$\begin{array}{r} 6x + 1.50y = 822 \\ x + y = 371 \\ \hline 5x = 1404 \\ x = 280.8 \end{array}$$

$$\begin{array}{r} 6(371 - y) + 1.50y = 822 \\ 2226 - 6y + 1.50y = 822 \\ -4.5y = -1404 \\ y = 312 \end{array}$$

59 \$1.50 tickets were sold

9. George saves nickels and dimes for tools. If he has 28 coins worth \$2.60, how many are nickels and how many are dimes?

$$\begin{array}{l} n - \# \text{ of nickels} \\ d - \# \text{ of dimes} \end{array}$$

$$\begin{array}{r} 0.10d + 0.05n = (2.60) \quad 10 \\ d + n = 28 \\ \hline -0.05d - 0.05n = -2.6 \\ \hline 0.05n = 2 \\ n = 40 \end{array}$$

$$\begin{array}{r} d + n = 28 \\ -4 \quad -4 \\ d = 24 \end{array}$$

4 nickels and 24 dimes.

Age Problems

10. Cordell is twice as old as Beth. Eight years ago he was 3 times as old. How old are Cordell and Beth now?

$$\begin{array}{l} C - \text{Cordell's age} \\ B - \text{Beth's age} \end{array}$$

$$\begin{array}{r} C = 2B \\ C - 8 = 3(B - 8) \\ 2B - 8 = 3(B - 8) \\ 2B - 8 = 3B - 24 \\ -B = -16 \\ B = 16 \\ C = 32 \end{array}$$

Cordell is 32 & Beth is 16.

11. In two years Peter will be twice as old as his sister Joyce. The sum of their present ages is 26. How old are Peter and Joyce?

$$\begin{array}{l} P - \text{Peter's age} \\ J - \text{Joyce's age} \end{array}$$

$$\begin{array}{r} P + 2 = 2(J + 2) \\ P + J = 26 \\ \hline P = 26 - J \\ 26 - J + 2 = 2(J + 2) \\ 28 = 3J + 4 \\ -4 \quad -4 \\ 24 = 3J \\ J = 8 \\ P = 18 \end{array}$$

Peter is 18 and Joyce is 8.

12. Six years ago Bill was 17 years younger than twice Ann's age. Now their combined age is 100 years. Find their present ages.

$$\begin{array}{l} B - \text{Bill's age} \\ A - \text{Ann's age} \end{array}$$

$$\begin{array}{r} B - 6 = 2(A - 6) - 17 \\ B + A = 100 \\ \hline B = 100 - A \\ 100 - A - 6 = 2A - 12 - 17 \\ 94 = 3A - 29 \\ +29 \quad +29 \\ 123 = 3A \\ A = 41 \\ B = 59 \end{array}$$

Ann is 41 and Bill is 59.